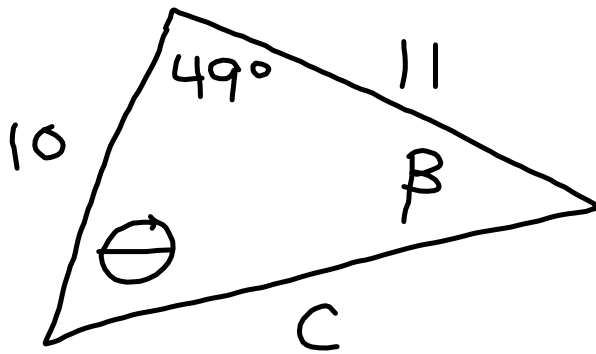


Feb. 27, 2017

Solve the triangle



$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$c^2 = 10^2 + 11^2 - 2(10)(11) \cos 49^\circ$$

$$c^2 = 76.67 \dots$$

$$\boxed{c = 8.76}$$

$$\frac{\sin \theta}{11} = \frac{\sin 49^\circ}{8.76}$$

$$\sin \theta = \frac{11 \cdot \sin 49^\circ}{8.76}$$

$$\theta = \sin^{-1} \left( \frac{11 \cdot \sin 49^\circ}{8.76} \right)$$

$$\boxed{\theta = 71.5^\circ}$$

$$\beta = 180^\circ - 71.5^\circ - 49^\circ$$

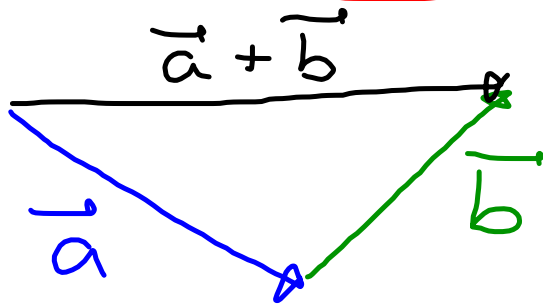
$$\boxed{\beta = 59.5^\circ}$$

# Addition and Subtraction of Vectors

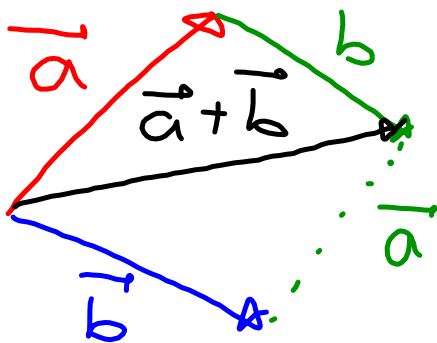
## Vector Addition

Consider two vectors  $\vec{a}$  and  $\vec{b}$ . When vectors are added they are added tip to tail and the resultant is  $\vec{a} + \vec{b}$

## Triangle Method of Adding Vectors



## Parallelogram Method



## Subtracting Vectors

From Friday, the **opposite** vector has the same magnitude and opposite direction.

To subtract  $\vec{u} - \vec{v}$ ,  
we change to  $\vec{u} + (-\vec{v})$ .

Change the direction of  $\vec{v}$   
then add the vectors.

## Opposite Vectors and the Zero Vector

$$3 + (-3) = 0$$

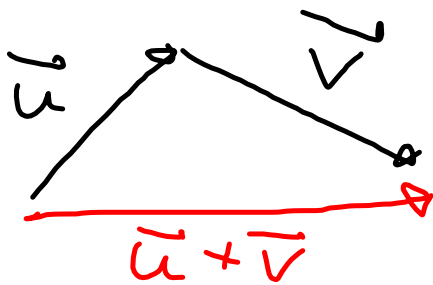
$$\vec{u} + (-\vec{u}) = \vec{0}$$

The zero vector  $\vec{0}$   
has no magnitude and  
no direction.

$$\vec{u} + \vec{0} = \vec{u}$$

## Commutative Property for Vector Addition

$$\vec{u} + \vec{v} = \vec{v} + \vec{u}$$



## Associative Property

$$\vec{u} + (\vec{v} + \vec{w}) = (\vec{u} + \vec{v}) + \vec{w}$$

Vectors can be added in any order.

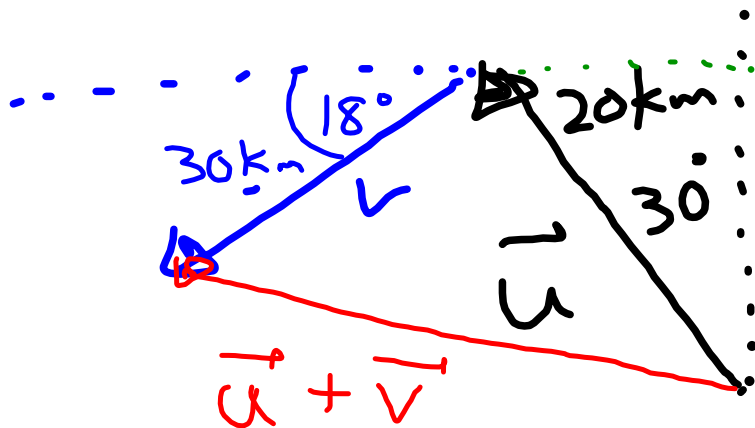
Ex. 1: If  $\vec{u} = 20\text{km} [N30^\circ W]$

$\vec{v} = 30\text{km} [W18^\circ S]$ ,

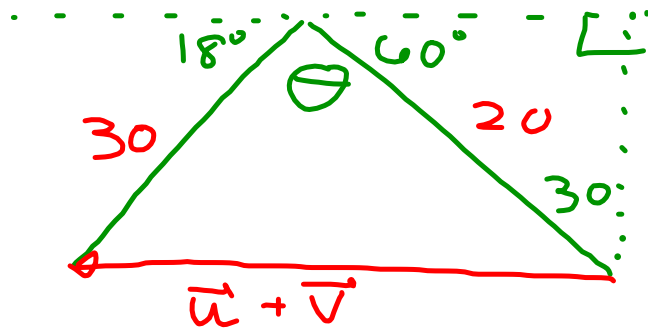
$\vec{w} = 40\text{km} [S22^\circ E]$  sketch

and find

a)  $\vec{u} + \vec{v}$







$$\Theta = 180^\circ - 60^\circ - 18^\circ$$

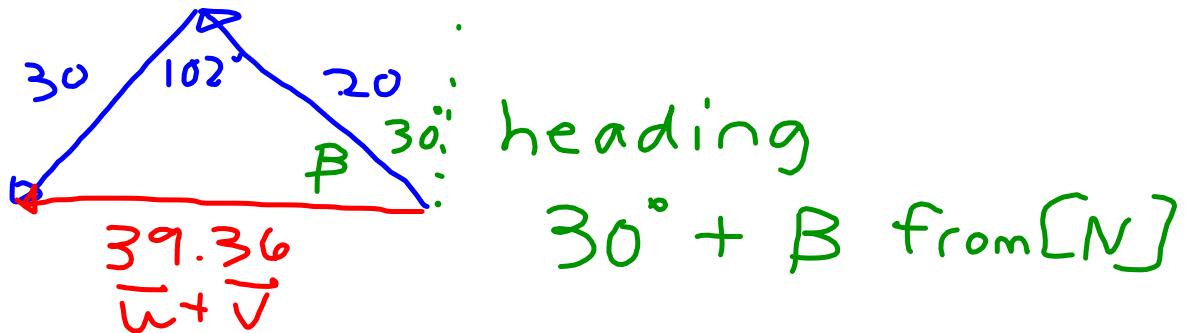
magnitude

$$\Theta = 102^\circ$$

$$|\vec{u} + \vec{v}|^2 = 30^2 + 20^2 - 2(30)(20)\cos 102^\circ$$

$$|\vec{u} + \vec{v}|^2 = 1549.5 \dots$$

$$|\vec{u} + \vec{v}| = 39.36 \text{ km}$$



$$\frac{\sin \beta}{30} = \frac{\sin 102^\circ}{39.36}$$

$$\sin \beta = \frac{30 \cdot \sin 102^\circ}{39.36}$$

$$\boxed{\beta = 48.1^\circ}$$

$$[N 30 + 48.1^\circ W]$$

$$[N 78.1^\circ W]$$

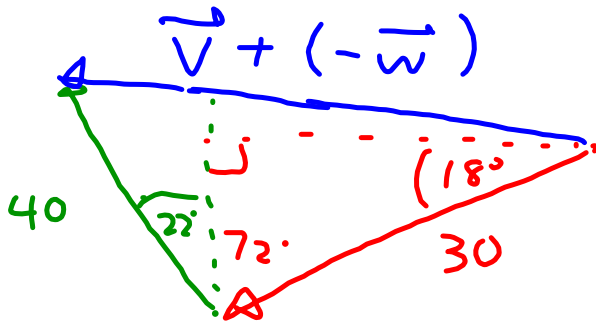
$$\vec{u} + \vec{v} = 39.36 \text{ km } [W 11.9^\circ N]$$

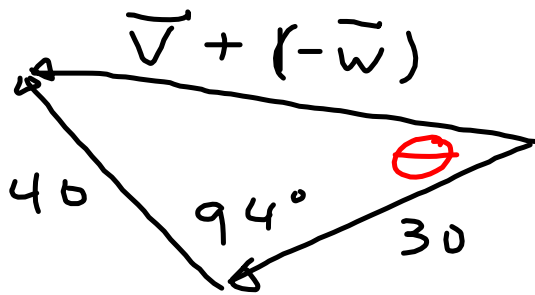
$$\vec{V} - \vec{W}$$

$$\vec{V} = 30 \text{ km [W } 18^\circ \text{ S]}$$

$$\vec{W} = 40 \text{ km [S } 22^\circ \text{ E]}$$

$$-\vec{W} = 40 \text{ km [N } 22^\circ \text{ W]}$$





$$|\vec{v} + (-\vec{w})|^2 = 40^2 + 30^2 - 2(40)(30)\cos 94$$

$$|\vec{v} + (-\vec{w})|^2 = 2667.416 \dots$$

$$\boxed{|\vec{v} + (-\vec{w})| = 51.6}$$

heading [W  $\theta$  - 18° N]

$$\frac{\sin \theta}{40} = \frac{\sin 94}{51.6}$$

$$\sin \theta = \frac{40 \cdot \sin 94}{51.6}$$

$$\boxed{\theta = 50.7^\circ}$$

$$\therefore \vec{V} + (-\vec{W}) = 51.6 \text{ km [W } 32.7^\circ \text{ N]}$$

HW p. 325

# 5, 6, 7, 9, 11, 14, 15, 16